GLOBAL SEISMIC OSCILLATIONS IN SOFT GAMMA REPEATERS

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ABSTRACT

There is evidence that soft gamma repeaters (SGRs) are neutron stars that experience frequent starquakes, possibly driven by an evolving, ultrastrong magnetic field. The empirical power-law distribution of SGR burst energies, analogous to the Gutenberg-Richter law for earthquakes, exhibits a turnover at high energies, consistent with a global limit on the crust fracture size. With such large starquakes occurring, the significant excitation of global seismic oscillations (GSOs) seems likely. Moreover, GSOs may be self-exciting in a stellar crust that is strained by many randomly oriented stresses. We explain why low-order toroidal modes, which preserve the shape of the star and have observable frequencies as low as ~30 Hz, may be especially susceptible to excitation. We estimate the eigenfrequencies as a function of stellar mass and radius, as well as their magnetic and rotational shifting/splittings. We also describe ways in which these modes might be detected and damped. There is marginal evidence for 23 ms oscillations in the hard initial pulse of the 1979 March 5 event. This could be due to the t0 mode in a neutron star with B ~ 1014 G or less, or it could be the fundamental toroidal mode if the field in the deep crust of SGR 0526–66 is ~4 × 1015 G, in agreement with other evidence. If confirmed, GSOs would give corroborating evidence for crust-fracturing magnetic fields in SGRs: B ≥ 1014 G.

Subject headings: stars: magnetic — stars: neutron — stars: oscillation — X-rays: stars

1. INTRODUCTION

Global shear modes in the Earth were first detected following the devastating Chilean earthquake of 1960 May (Benioff, Press, & Smith 1961). The fundamental toroidal mode, which for m = 0 involves a simple, alternating, periodic twisting of whole hemispheres in opposite directions, has a period of 43 minutes in the Earth. In general, the toroidal modes are pure shear deformations, divergence-free, with no radial components. They are referred to by the notation t0, where the overtone number n is the number of radial nodes in the eigenfunctions (e.g., McDermott, Van Horn, & Hansen 1988, hereafter MVHH).

Any condensed object with a solid component can support shear modes. For example, old white dwarfs with crystalline cores have P(t0) ≈ 12 s (Hansen & Van Horn 1979), but in this case, the solid core lies within an opaque, liquid mantle, so detection is problematic. Neutron stars, which have fractionally thin solid crusts floating on mantles of superfluid, offer better prospects for supporting observable shear modes. Because the crusts are thin and subject to little friction from below, large-amplitude shear oscillations could be excited with much less energy than would be required in true solid bodies. Moreover, substantial modal deformation occurs at, or very near, the observable surface.

The toroidal (or torsion) modes, which preserve the star’s shape, may be especially easy to excite via starquakes, because the restoring force for these modes is entirely due to the relatively weak Coulomb forces of the crustal ions as given by the shear modulus: μ ~ (Ze)^2/na^2, where a is the ion spacing. Other internal modes involve bulk compression and vertical motion, which have to do work against the much stronger degeneracy pressure of electrons in the outer crust and free neutrons in deeper layers, as well as gravity. This implies that (1) toroidal shear deformations require much less energy than do radial or compressional deformations of comparable amplitude and (2) low-order t-modes also have unusually low frequencies. Since the damping rate (e.g., via coupling to Alfven modes in the magnetosphere or other mechanisms; see § 3 below) generally increases steeply with oscillation frequency, both of these circumstances favor the significant excitation of low-order t-modes.

For many—or all—of these reasons, shortly after the discovery of pulsars, Ruderman (1968) proposed that the radio pulsations found by Hewish et al. (1968) were due to the fundamental toroidal mode, t0, in a neutron star. We now know that spin-down–driven seismic activity is possible in ordinary pulsars (e.g., Ruderman 1991), but it has not proved sufficient to excite detectable crust vibrations. However, there is another class of stars in which Ruderman’s prescient proposal might more readily apply: soft gamma repeaters (SGRs).

A variety of evidence seems to indicate that SGRs are neutron stars that experience strong and frequent starquakes (e.g., Thompson & Duncan 1995 and 1996, hereafter TD95 and TD96, respectively). Comparative analyses of SGR and earthquake records (Cheng et al. 1996) indicate that the relative distribution of SGR burst energies and waiting times, and their correlations, are consistent with crust fracture/slippage events, but not with any known accretion- or nuclear-powered phenomenon. This accords with the hypothesis that SGRs are neutron stars with ultrastrong magnetic fields: B ≫ m_e c^2/eh = 4.4 × 10^{13} G. Under this hypothesis, SGR bursts are the observable signature of starquakes driven by the stresses of an evolving magnetic field, and the exceptionally energetic 1979 March 5 event is identified as a magnetic flare (Duncan & Thompson 1992, hereafter DT92; Paczyński 1992; TD96). Such magnetically active neutron stars, or magnetars, could form as a result of α2 dynamos in hot, newborn neutron stars undergoing convective mixing (e.g., Keil, Janka, & Müller 1996), if they are born rotating more quickly than the relevant “dynamo number” threshold (DT92; Thompson & Duncan 1993, hereafter DT93; Duncan & Thompson 1996, hereafter DT96). It is even possible that some magnetars form without strong convection (e.g., following rotation-supported core
bounce) because differential rotation, which is generic for high angular momentum proto–neutron stars, could alone generate fields $\sim 10^{14} (P_\text{rot}/1 \text{ ms})^{-1} \text{ G}$, where $P_\text{rot}$ is the rotation period (DT92; TD93; DT96). Seven different estimates of the field in SGR 0526–66 indicate that $B \gtrsim 10^{14} \text{ G}$ ($\S$ 1 in TD95).

We now consider the physics of global seismic$^1$ oscillations (GSO) in SGRs. We will focus on $t$-modes, although our results on excitation and damping could apply to other crustal modes (e.g., $s$-modes) as well.

2. EIGENFREQUENCIES AND STRAIN AMPLEUDIES

The fundamental toroidal mode’s period is roughly given by the time for a shear wave to travel around the star: $P \sim R/V_\nu$, where $V_\nu = (\mu/\rho)^{1/2}$ is the shear wave velocity. This crude estimate ignores vertical structure in the crust, but this is a surprisingly good approximation because $V_\nu$ varies only weakly with depth (Ruderman 1968; Strohmayer et al. 1991). Accurate mode calculations have been done by Hansen & Cioffi (1980) and MVHH. The separation of variables for the shear wave equation, subject to the $t$-mode conditions $u_r = 0$ and $\nabla \cdot u = 0$, gives solutions of the form

$$u_\theta = \frac{W(r) \partial Y_{\text{nm}}}{\sin \theta \partial \phi}, \quad u_\phi = -W(r) \frac{\partial Y_{\text{nm}}}{\partial \theta},$$

(1)

where $(u_\theta, u_\phi, u_r)$ are displacement amplitudes in spherical coordinates, and $Y_{\text{nm}}(\theta, \phi)$ are spherical harmonics. For $n = 0$ modes, the radial eigenfunctions $W(r)$ vary little with depth in the crust (MVHH).

The results of MVHH’s model calculations are given in columns (1) and (3) of Table 1. Note that the neutron star radii listed here are smaller than generally thought realistic for their respective masses, because MVHH used an interior (subcrust) equation of state that is probably unrealistically soft. We now seek to estimate the observable eigenperiod for a canonical $M = 1.4 M_\odot$, $R = 10$ km neutron star (Table 1, col. [2]), as well as its dependence on $M$ and $R$. To do this, note that the structure of the crust depends on $M$ and $R$ almost entirely through the action of the surface acceleration of gravity, hence so will the effective (depth-averaged) $V_\nu$. The quantity $P/R \propto V_\nu^{-1}$ (Table 1, row [4]) should therefore be a function of $g = GM/R^2$ (row [5]; tabulated in units of $10^{14}$ cm s$^{-2}$), so we interpolate over $g$ to estimate $P/R$ and $P$ (col. [2]). Two further corrections are needed. Improved calculations of $\mu$ (Strohmayer et al. 1991), including directionally averaging (Ogata & Ichimaru 1990), imply that $P \propto \mu^{-1/2}$ is actually larger by 1.24 than found by MVHH, as quoted in Table 1. Gravitational time dilation further increases the observable period. We find

$$P_{(5t_0)} = 33.6 R_{10}^{0.87} M_{1.4}^{0.13} R_{10}^{-2} \left(1.71 - 0.71 M_{1.4} R_{10}^{-2}\right)^{1/2} \text{ ms},$$

(2)

where $R_{10} = (R/10 \text{ km})$ and $M_{1.4} \equiv (M/1.4 M_\odot)$.

For higher order modes, the period scales as $P_{\ell t_0} \propto [(\ell + 1)^{1/2}]^{-1/2}$ (e.g., Hansen & Cioffi 1980), so the predicted mode spectrum, in units of milliseconds, is roughly $P \approx 34, 24, 18, 15 \ldots$. Each of these modes is $(2\ell + 1)$-fold degenerate in $m$. (In $\S$ 4, we consider magnetic and rotational shifting and splitting of the eigenfrequencies.) Overtone modes ($n > 0$) have much shorter periods, on the order of a few milliseconds or less (e.g., MVHH).

The mode energy scales roughly as $E_m \propto R^4/M$ since the elastic deformation energy per unit area of crust scales as $g^{-1}$ in hydrostatic equilibrium (eq. [6] below). Thus, the quantity $EM/R^4$ is nearly constant in MVHH’s models (Table 1, row [7]), where $E \equiv E_m [W(R)/R]^{-2}$ (row [6]; tabulated in units of $10^{48}$ ergs). Interpolating over $g$ again, and including the correction factor to $\mu$, we find

$$E_m = 5 \times 10^{47} \frac{[W(R)]^2}{R} \times R_{10}^4 M_{1.4}^{-1} (0.77 + 0.23 M_{1.4} R_{10}^{-2}) \text{ ergs},$$

(3)

for the $2t_0$ mode energy. The surface displacement amplitude for $m = 0$ is then given by equation (1):

$$u_\theta = 440 E_m^{1/2} R_{10}^{1/2} M_{1.4}^{1/2} \sin \theta \text{ cm},$$

(4)

where $E_m \equiv (E_m/10^{48} \text{ ergs})$. [For simplicity, we omit the fine adjustment factor $(0.77 + 0.23 M_{1.4} R_{10}^{-2})$ in this and the following equation.] The amplitude of the modal strain is

$$\psi_m = 0.9 \times 10^{-3} E_m^{1/2} R_{10}^{3/2} M_{1.4}^{1/2} \sin^2 \theta.$$  

(5)

For $m \neq 0$, the angular distribution of the strain is different, but the amplitude is comparable.

Equation (5) is a remarkable result, because (1) the observed, prompt X-ray energy of a single bright SGR burst is $\sim 10^{44}$ ergs (e.g., Norris et al. 1991), so the energy of a major starquake must be comparable to or larger than this; and (2) the static critical (yield) strain of a neutron star crust is probably in the range $\psi_m \sim 10^{-3}$ and perhaps less (Smoluchowski & Welch 1970; Ruderman 1991). (Although $\psi_m \sim 10^{-2}$ in a pure bcc Coulomb crystal, realistic crustal material is almost certainly weakened by lattice dislocations.) Thus, if a seismic episode, involving multiple starquakes, imparts to the mode even a minor fraction of the X-ray energy of a single bright burst, then the modal strains themselves will be large enough to trigger starquakes at other sites in the crust that have preexisting (magnetically induced) strains significantly less than $\psi_m$. These triggered events can give impetus to the mode, as we now explain.

3. MODE EXCITATION, DAMPING, AND DETECTABILITY

The energy of an event in which critical strains are relieved throughout an area $A$ of the crust is $e = (1/2)\mu A \xi \mu dz$.
where the integral runs over the depth of the fracture and \( \xi > 1 \) accounts for released magnetic (as opposed to elastic) energy. [This satisfies \( \xi < (4\pi\mu B^2)/10B_{\xi}^2 \), except when there is significant reconnection; § 2.2 in TD95.] Using the equation of state of Negele & Vautherin (1973) to evaluate the integral down to the base of the crust, we find

\[
e = 4.2 \times 10^{38} i^2 \psi_{\epsilon_{3}} R_{10}^2 M_{14}^{-1} \text{ ergs,}
\]

where \( \psi_{\epsilon_{3}} \equiv (\psi_{\epsilon}/10^{-7}) \), and we take \( A = l_f^2 \) for a fracture of length \( l_f = 1 \text{ km} \). This result scales as \( g^{-1} \propto R^2 M^{-1} \) because \( dz = (\rho g)^{-1} dP \) in hydrostatic equilibrium.

The empirical burst energy distribution for SGR 1806–20 is a power law with index \( \gamma = 1.66 \) (Cheng et al. 1996), analogous to the Gutenberg-Richter law for earthquakes (Gutenberg & Richter 1956). This is a natural consequence of self-organized criticality (e.g., Bak 1996). Unlike the case of earthquakes, the SGR burst distribution turns over at high \( \epsilon \), with an apparent upper limit \( \epsilon_{\text{max}} = 3 \times 10^{14} D_{14}^2 \text{ ergs, for SGR 1806–20} \) at a distance \( D = 14 D_{14} \text{ kpc from Earth} \) (Corbet et al. 1997). If this is due to a maximum fracture scale, \( l_{\text{max}} \), then

\[
(l_{\text{max}}/2\pi R) = 0.4\psi_{\epsilon_{3}}^{-1} \xi^{-1/2} f^{-1/2} R_{10}^{-2} M_{14}^{1/2} D_{14}.
\]

where \( f \lesssim 1 \) is the fraction of the released energy that powers burst emissions. This suggests that the observed turnover in the SGR burst energy distribution is due to global limits on the fracture size. For comparison, the largest earthquakes yet measured by modern seismographs have dimensions \((l_{\text{max}}/2\pi R_{\text{earth}}) < 10^{-3}\) (Scholz 1990).

Global fractures propagate across the crust on timescales \( R/V_{\epsilon} \), comparable to the period of low-order seismic modes, which are thus readily excited. Once GSOs begin, new fractures can be triggered, but always as the modal strain is locally increasing with a component in the direction of the preexisting (magnetic) strain. Each of these triggered fractures can give an energy boost to the mode, for reasons that may be understood via a simple one-dimensional analogy. Imagine that a rubber band is stretched to near its breaking point and held. This requires energy, say, from person A, who stretches the rubber band; thus, person A plays a role analogous to the magnetic field. Another person, B, grasps the band just within person A’s fingers and imparts a further, small-amplitude periodic stretching, as done by the GSO. When the band breaks, it snaps against person B’s fingers, giving an impulse in the direction of person B’s motion (a mode-boosting impulse). The energy released is much greater than the energy of stretching by person B (the mode); it ultimately comes from person A (the magnetic field) as stored in the elastic band (the crustal strain). After the band breaks, person A might also do additional work in dragging person B’s fingers apart. This is the effect quantified by \( \xi \) above. It depends on the fault slippage, which is difficult to estimate (§ 2.2 in TD95).

This analogy suggests that GSOs are potentially self-exciting in a stellar crust with many randomly oriented strains. Indeed, for a power-law distribution of preexisting strains, \( \Delta^2 N_{\text{random}} \psi \propto \psi^g \), and for an excitation efficiency \( \epsilon = \epsilon \psi \), self-sustaining mode growth occurs to modal strain amplitudes

\[
\psi_{\epsilon} \sim (\psi_{\epsilon})_{\text{crit}} \text{ if } \epsilon > \chi \psi_{\epsilon}(1 + \psi_{\epsilon})^{-1}(1 - \psi_{\epsilon})^{-(\alpha + 1)},
\]

where \( \Delta \) is the fraction of the star’s surface area that is strained. The SGR “Gutenberg-Richter law” (Cheng et al. 1996) implies \( \alpha = 2.32 \) if most fractures occur when \( \psi_{\epsilon} = \psi_{\epsilon} - \psi_{\epsilon} \ll \psi_{\epsilon} \). As long as \( \beta > \alpha - 3 \approx -0.68 \), large fractures dominate the excitation. This is probably true since large fractures tend to be more efficient at excitation than small fractures, i.e., \( \beta > 0 \). For \( \beta = 1 = \alpha \) and \( \psi_{\epsilon} \ll 1 \), the efficiency criterion is \( \epsilon_{\text{crit}} \approx 0.002(\psi_{\epsilon}/0.1)\psi_{\epsilon}\Delta^{-1} \xi^{-1/2} R_{10}^{-2} M_{14}^{1/2} \). This suggests that terminal mode amplitudes \( \sim \psi_{\epsilon} \), could be attained by self-sustained mode growth.

When excitation is dominated by large fractures, it is possible that only a few low-order modes are substantially excited. For high-(\( l, m \)) modes, a randomly oriented fault line can traverse modal zones with changing senses of strain, which tends to hamper excitation. As starquakes are triggered, the mode axis will wander (since excitation amplitudes add in phase like axial vectors), allowing strains to be released all over the crust. Thus, modes that happen to be excited by a spontaneous starquake at the start of a seismic episode could grow rapidly, leaving little elastic/magnetic energy to be tapped by other modes.

How might GSOs be detected? SGR burst emissions could be significantly modulated at the mode period. For example, a large crust fracture, once began, could extend in length each time the mode stresses it the right way, producing new pulses of Alfvén waves, pair creation, and observable X-rays during each GSO cycle (see § 2 in TD95). Alternatively, there may be detectable discreteness in the time spacings of the aftershock-like events following a bright burst (Kouveliotou et al. 1996), if these are triggered by the mode rather than by the general redistribution of stress. Since triggering usually occurs near but just before the two instants of maximum deformation in the mode cycle, the expected time intervals between mode-triggered burst are \( \Delta t = \eta (R/2) \), where \( \eta \) is an integer. This is especially true for \( \eta \geq P \). When \( \Delta t \gg P \), especially over intervals containing bursts, modal phase drift would mask the effect.

How do GSOs damp? There are several possible mechanisms; here we will concentrate on fault line slippage and refractoring. Like the Earth, a neutron star is probably laced with fault lines, along which the effective critical strain is smaller than usual: \( \epsilon_{\text{crit}} < \epsilon_{\text{crit}} \). These may be sites of recent fractures that have not fully healed (in which case \( \epsilon_{\text{crit}} \) is actually the threshold for slipping against friction rather than a true yield strain; Sholz 1990) or areas where magnetic stresses have a history of accumulating and weakening the crust. Whenever the mode strain amplitude along the fault line, \( \psi_{\epsilon,\text{f}} \), exceeds \( \psi_{\epsilon,\text{f}} \), then slippage occurs, as often as \( 2\psi_{\epsilon,\text{f}}/\epsilon_{\text{crit}} \) times per cycle when this number exceeds 2. This “sticky” motion reprocesses mode energy, mostly into seismic waves of peak frequency \( \sim V_{\epsilon}/\epsilon \), which is in the kilohertz range for \( l \sim 1 \text{ km} \), comparable to the depth of the crust. Such high-frequency waves couple strongly to Alfvén modes in the lower magnetosphere (TD95; Thompson & Blaes 1997), while low-frequency ones are internally reflected (Blaes et al. 1989; Duncan et al. 1998). Each reslippage/refracting event thus injects energy into the magnetosphere, maintaining an X-ray-emitting
plasma there. The resultant mode damping time, $\tau$, is difficult to estimate, but if $\tau < 130$ $E_{\gamma} F_1^{-1} (D/8 \text{ kpc})^{-3} \text{ s}$, where $F_1 = 10^{-2} \text{ F}_1$; ergs cm$^{-2}$ s$^{-1}$ is the X-ray detector threshold, then the energy of GSO damping would be detectable as quasi-steady X-rays during active episodes, fading after bursts cease. Such emissions could be detectable even if many different seismic modes are excited.

4. MAGNETIC FREQUENCY SHIFTS AND THE MARCH 5 EVENT

If a tangled magnetic field of rms strength $B$ is embedded throughout the crust, then magnetic tension augments $\mu$, and

$$P \approx P_0 \left[ 1 + \left( B/B_p \right)^2 \right]^{-1/2},$$

(9)

where $P_0$ is the nonmagnetic period (eq. [2], in the case of $2f\text{ br}$), and $B_p = (4\pi \mu)^{1/2} \approx 4 \times 10^{13} \mu_{14}^4 \text{ G}$, based on a power-law fit to the deep-crust ($\rho > \rho_{\text{dep}} = 4.6 \times 10^{13} \text{ g cm}^{-3}$) equilibrium composition found by Negele & Vautherin (1973). Note that the mode energy (eq. [3]) also shifts upward by a factor $[1 + (B/B_p)^2]$.

Even if $B \ll B_p$ in the deep crust, near the star’s surface, at densities $\rho < 4 \times 10^{10} \mu_{14}^{1/2} \text{ g cm}^{-3}$ for $B_{14} < 4$, magnetic restoring forces exceed elastic ones. This perturbs the eigenfunctions in the outer layers of the crust, but it has little effect on the observable GSO period since the great preponderance of mode deformation energy (or kinetic energy) resides below this (Carroll et al. 1986). Thus, it is appropriate to take $\rho_{14} \sim 1$ in the formula for $B$, when evaluating equation (9) (except in the Alfvén limit, $B \gg B_p$, for which eq. [9] no longer applies).

Magnetic frequency shifts also can split the eigenfrequencies, resolving the $(2F + 1)$-fold degeneracy in $m$. Equation (9) is precisely accurate only in the case of a disordered field uniformly penetrating the star’s crust. A realistic field with global structure will produce $m$-dependent shifts of order $\Delta P/P \sim (B/B_p)^2$ for $B \ll B_p$, where the precise splittings depend on field geometry and mode orientation. Rotational splittings $\Delta P/P = [m/(\ell + 1)]P_{\text{rot}}$ also occur (Lapwood & Usami 1981; Strohmayer 1991). However, for $f_{\text{br}}$, this is only $\Delta P/P = 7 \times 10^{-4} m(P_{\text{rot}}/8.0 \text{ s})^{-1}$, where we scale to the rotation period of SGR 0526−66 as inferred from the 1979 March 5 event. For comparison, rotational splittings of $m$-modes are~10 times larger in the Earth, yet they have not been detected (Lay & Wallace 1995).

The exceptionally energetic 1979 March 5 event was probably due to a large-scale instability in a magnetar (§ 2.1 of TD95). A likely candidate is the Flowers-Ruderman instability, which involves a global crust fracture and a (small-angle) relative twist of two sections of crust, diminishing the exterior dipole moment as reconnection powers the flare (Flowers & Ruderman 1977; §§ 14.2 and 15.2 in TD93). This would excite very strong GSOs. Indeed, there is evidence for a 23 ms periodicity in the hard initial pulse of the event (Barat et al. 1983). This could be due to $f_{\text{br}}$ oscillations in a neutron star with $B \approx 10^{13} \text{ G}$, or it could be due to the fundamental mode, $f_{\text{br}}$, if the field in the deep crust is $B = 1.06 B_{14} \approx 4 \times 10^{13} \text{ G}$, for a $1.4 M_{\odot}$, 10 km neutron star (eqs. [2] and [9]). Such strong fields in the deep crust of SGR 0526−66 have previously been inferred for other reasons (TD95; TD96). Note that several modes would probably be excited by such a catastrophe, and the ongoing release of energy would also affect crustal motions, so a complex (nonsinusoidal) light curve is to be expected.

In conclusion, if SGR bursts are due to starquakes, then strong seismic waves almost certainly vibrate SGR crusts during active episodes. Whether a few low-order GSOs can attain sufficient amplitudes to have detectable consequences is less certain. We have given three reasons why this is at least possible: (1) global-sized fractures (eq. [7]) naturally excite lower-order modes; (2) mode damping, via Alfvén wave loss and other mechanisms, declines steeply with frequency; and (3) the “self-exciting” effect could drive runaway growth of single modes.

If the presence of GSOs in SGRs, as suggested by the 1979 March 5 data, is verified by future observations, this will add to the (already considerable) evidence for seismic activity in these stars. Magnetism is a natural candidate for driving this activity, especially in light of the other evidence for very strong fields in SGRs (as summarized in § 1 of TD95). Rotational energy may trigger some starquakes and glitches in ordinary pulsars (e.g., Ruderman 1991), but this could not power SGR activity in a neutron star with an 8.0 s period like SGR 0526−66. Magnetars seem necessary, because typical pulsar-strength fields could not drive strains in excess of $\psi_c$ and fracture the crust. Hooke’s law requires

$$B \approx \left( 4\pi \mu \psi_c \right)^{1/2} = 1.2 \times 10^{14} \rho_{14}^{0.4} \left( \frac{\psi_c}{10^{-7}} \right)^{1/2} \text{ G},$$

(10)

where $\rho_{14} \sim 1$ because only deep fractures have sufficient energy to power bright SGR bursts (eqs. [6]–[7]).

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